

# Webcam-based Visual Gaze Estimation

Roberto Valenti<sup>1</sup>, Jacopo Staiano<sup>1</sup>, Nicu Sebe<sup>2</sup>, Theo Gevers<sup>1</sup>

<sup>1</sup>Faculty of Science, University of Amsterdam, The Netherlands  
{rvalenti,staiano,gevers}@science.uva.nl

<sup>2</sup>University of Trento, Italy  
sebe@disi.unitn.it

**Abstract.** In this paper we combine a state of the art eye center locator and a new eye corner locator into a system which estimates the visual gaze of a user in a controlled environment (e.g. sitting in front of a screen). In order to reduce to a minimum the computational costs, the eye corner locator is built upon the same technology of the eye center locator, tweaked for the specific task. If high mapping precision is not a priority of the application, we claim that the system can achieve acceptable accuracy without the requirements of additional dedicated hardware. We believe that this could bring new gaze based methodologies for human-computer interactions into the mainstream.

## 1 Introduction

Eye location and tracking and the related visual gaze estimation are important tasks in many computer vision applications and research [1]. Some of the most common examples are the application to user attention and gaze in driving and marketing scenarios, and control devices for disabled people. Eye location/tracking techniques can be divided into three distinct modalities [2]: (1) Electro oculography, which records the electric potential differences of the skin surrounding the ocular cavity; (2) scleral contact lens/search coil, which uses a mechanical reference mounted on a contact lens, and (3) photo/video oculography, which uses image processing techniques to locate the center of the eye. Unfortunately, the common problem of the above techniques is the use of intrusive and expensive sensors [3]. While photo/video oculography is considered the least invasive of the modalities, commercially available trackers still require the user to be either equipped with a head mounted device, or to use a high resolution camera combined with a chinrest to limit the allowed head movement. Furthermore, daylight applications are precluded due to the common use of active infrared (IR) illumination, used to obtain accurate eye location through corneal reflection. Non infrared appearance based eye locators [4–11] can successfully locate eye regions, yet are unable to track eye movements accurately.

The goal of this paper is to present a way to map eye gaze patterns on a screen. These patterns are detected based on a few ingredients: (1) an eye tracker that can quickly and accurately locate and track eye centers and eye corners in low resolution images and videos (i.e., coming from a simple web

cam); (2) a scale space framework that gives scale invariance to the eye center and eye corners localization; and (3) a mapping mechanism that maps eye and corner locations to screen coordinates.

## 2 Isocenters Estimation

The isophotes of an image are curves connecting points of equal intensity. Since isophotes do not intersect each other, an image can be fully described by its isophotes. Furthermore, the shape of the isophotes is independent to rotation and linear lighting changes [12]. To better illustrate the well known isophote framework, it is opportune to introduce the notion of intrinsic geometry, i.e., geometry with a locally defined coordinate system. In every point of the image, a local coordinate frame is fixed in such a way that it points in the direction of the maximal change of the intensity, which corresponds to the direction of the gradient. This reference frame  $\{v, w\}$  is referred to as the *gauge coordinates*. Its frame vectors  $\hat{w}$  and  $\hat{v}$  are defined as:

$$\hat{w} = \frac{\{L_x, L_y\}}{\sqrt{L_x^2 + L_y^2}}; \hat{v} = \perp \hat{w}; \quad (1)$$

where  $L_x$  and  $L_y$  are the first-order derivatives of the luminance function  $L(x, y)$  in the  $x$  and  $y$  dimension, respectively. In this setting, a derivative in the  $w$  direction is the gradient itself, and the derivative in the  $v$  direction (perpendicular to the gradient) is 0 (no intensity change along the isophote). In this coordinate system, an isophote is defined as  $L(v, w(v)) = \text{constant}$  and its curvature  $\kappa$  is defined as the change  $w''$  of the tangent vector  $w'$  which in Cartesian coordinates becomes [13–15]:

$$\kappa = -\frac{L_{vv}}{L_w} = -\frac{L_y^2 L_{xx} - 2L_x L_{xy} L_y + L_x^2 L_{yy}}{(L_x^2 + L_y^2)^{3/2}}. \quad (2)$$

Since the curvature is the reciprocal of the radius, we can reverse Eq. (2) to obtain the radius of the circle that generated the curvature of the isophote. The radius is meaningless if it is not combined with orientation and direction. The orientation can be estimated from the gradient, but its direction will always point towards the highest change in the luminance. However, the sign of the isophote curvature depends on the intensity of the outer side of the curve (for a brighter outer side the sign is positive). Thus, by multiplying the gradient with the inverse of the isophote curvature, the duality of the isophote curvature helps in disambiguating the direction of the center. Since the gradient can be written as  $\frac{\{L_x, L_y\}}{L_w}$ , we have:

$$\begin{aligned} D(x, y) &= \frac{\{L_x, L_y\}}{L_w} \left( -\frac{L_w}{L_{vv}} \right) = -\frac{\{L_x, L_y\}}{L_{vv}} \\ &= -\frac{\{L_x, L_y\}(L_x^2 + L_y^2)}{L_y^2 L_{xx} - 2L_x L_{xy} L_y + L_x^2 L_{yy}}. \end{aligned} \quad (3)$$

where  $D(x, y)$  are the displacement vectors to the estimated position of the centers, which can be mapped into an accumulator, hereinafter “*centermap*”. Since every vector gives a rough estimate of the center, we can convolve the accumulator with a Gaussian kernel so that each cluster of votes will form a single center estimate. Furthermore, the contribution of each vector can be weighted according to a relevance mechanism. The main idea is that by collecting and averaging local evidence of curvature, the discretization problems in a digital image could be lessened and accurate center estimation could be achieved.

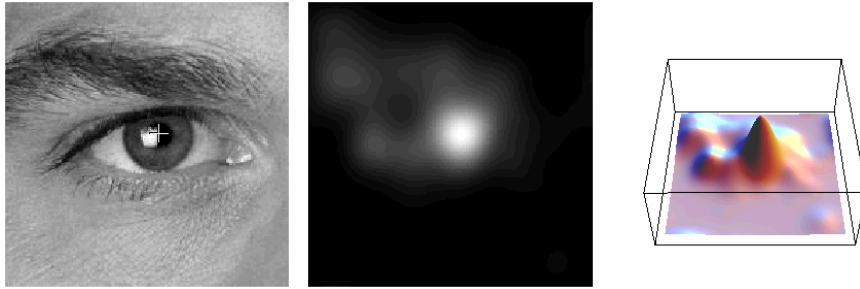
In order to achieve this goal, only the parts of the isophotes which are meaningful for our purposes should be used, that is, the ones that follow the edges of an object. This selection can be performed by using the curvedness [16]:

$$curvedness = \sqrt{L_{xx}^2 + 2L_{xy}^2 + L_{yy}^2}. \quad (4)$$

We note that the curvedness has low response on flat surfaces and edges, whereas it yields high response in places where the isophote density is maximal. As observed before, the isophote density is maximal around the edges of an object, meaning that by selecting the parts of the isophotes where the curvedness is maximal, they will likely follow an object boundary and locally agree on the same center. The advantage of this approach over a pure edge based method is that, by using the curvedness as the voting scheme for the importance of the vote, every pixel in the image may contribute to a decision. By summing the votes, we obtain high response on isocentric isophotes patterns which respect the constraint of being near edges. We call these high responses “*isocenters*”, or ICs.

### 3 Eye Center Location

Recalling that the sign of the isophote curvature depends on the intensity of the outer side of the curve, we observe that a negative sign indicates a change in the direction of the gradient (i.e., from brighter to darker areas). Therefore, it is possible to discriminate between dark and bright centers by analyzing the sign of the curvature. Regarding the specific task of cornea and iris location, it can be assumed that the sclera is brighter than the cornea and the iris, so we should ignore the votes in which the curvature is positive, that is, where it agrees with the direction of the gradient. As a consequence, the maximum isocenter (MIC) obtained will represent the estimated center of the eye. The result of this procedure on an eye image is shown in Figure 1. From the 3D plot it is clear where the MIC is, but we can expect that certain lighting conditions and occlusions from the eyelids to result in a wrong eye center estimate. To cope with this problem, we use the mean shift algorithm for density estimation. Mean shift (MS) usually operates on back-projected images in which probabilities are assigned to pixels based on the color probability distribution of a target, weighted by a spatial kernel over pixel locations. It then finds the local maximum of this distribution by gradient ascent [17]. Here, the mean shift procedure is directly



**Fig. 1.** The source image, the obtained centermap and the 3D representation of the latter

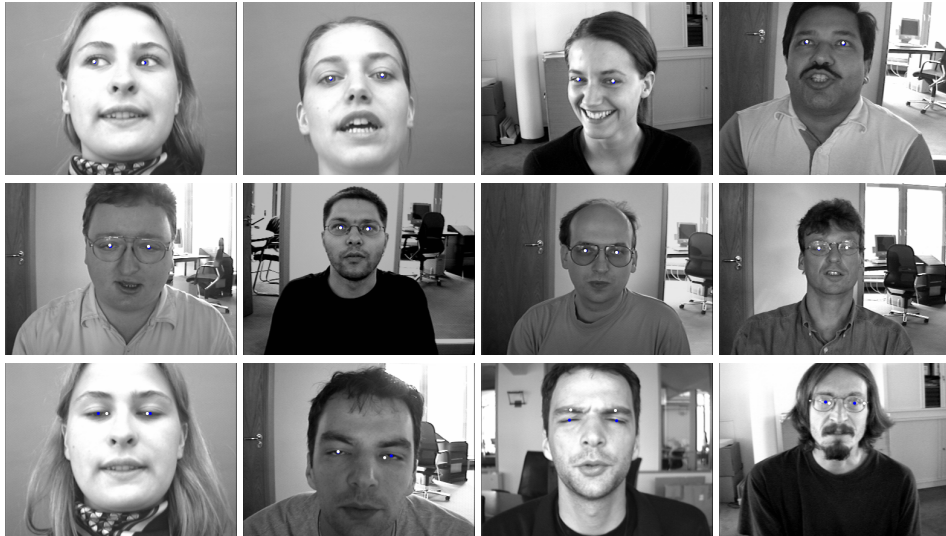
applied to the centermap resulting from our method, under the assumption that the most relevant isocenter should have higher density of votes, and that wrong MICs are not so distant from the correct one (e.g., on an eye corner). A mean shift search window is initialized on the centermap, centered on the found MIC. The algorithm then iterates to converge to a region with maximal votes distribution. After some iteration, the isocenter closest to the center of the search window is selected as the new eye center estimate.

An extensive evaluation of the eye locator was performed in [15], testing the eye locator for robustness to illumination and pose changes, for accurate eye location in low resolution images and for eye tracking in low resolution videos. The comparison with the state of the art suggested that the method is able to achieve highest accuracy, but this is somewhat bounded by the presence of a symmetrical pattern in the image.

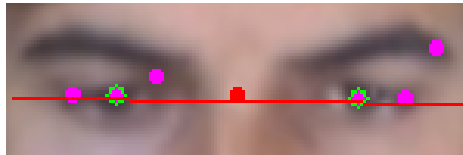
Figure 2 qualitatively shows some of the results obtained on different subjects of the BioID database. The dataset consists of 1521 grayscale images of 23 different subjects and has been taken in different locations and at different times of the day (i.e., uncontrolled illumination). We observe that the method successfully deals with slight changes in pose, scale, and presence of glasses (second row). By analyzing the failures (last row) it can be observed that the system is prone to errors when presented with closed eyes, very bright eyes, or strong highlights on the glasses. When these cases occur, the iris and cornea do not contribute enough to the center voting, so the eyebrows or the eye corners assume a position of maximum relevance.

## 4 Eye Corner Location

Unfortunately the eye center location is not enough for visual gaze estimation: there is a need for an accurate fixed point (or anchor point) in order to be able to measure successive displacements of the eye center independently of the face position. The common approach is to locate the position of the eyelids and the eye corners [18, 19]. A fast and inexpensive way to locate such an anchor is to reuse the obtained centermap. As stated before, by analyzing the results



**Fig. 2.** Sample of success and failures (last row) on the BioID face database; a white dot represents the estimated center.



**Fig. 3.** Eye centers and corner candidates

of the eye locator we note that the largest number of mistakes in eye-center location are located on eye corners. This is due to the fact that the eye corners have a somewhat symmetrical structure: in blurred low resolution imagery, the junction between the eyelashes creates an almost circular dark structure which is in contrast with the brighter skin and the sclera and therefore receives higher response than the rest of the features. In this way we can exploit this problem to our advantage. Figure 3 shows the highest ICs obtained. Once the eye center is selected by the mean shift we can apply some geometrical constraints to find the most stable anchor. Experimentally, the external eye corner turned out to be the most stable isocenter. In order to find them we look for the furthest away isocenter that lays closer to the line created by connecting the two eye centers (shown in red in Figure 3). While this assumption is reasonable and showed quite stable results (see Figure 4), the process is bound to fail every time that the eye locator fails (last image in Figure 4). This problem could be solved by enforcing additional constrains on the movement.

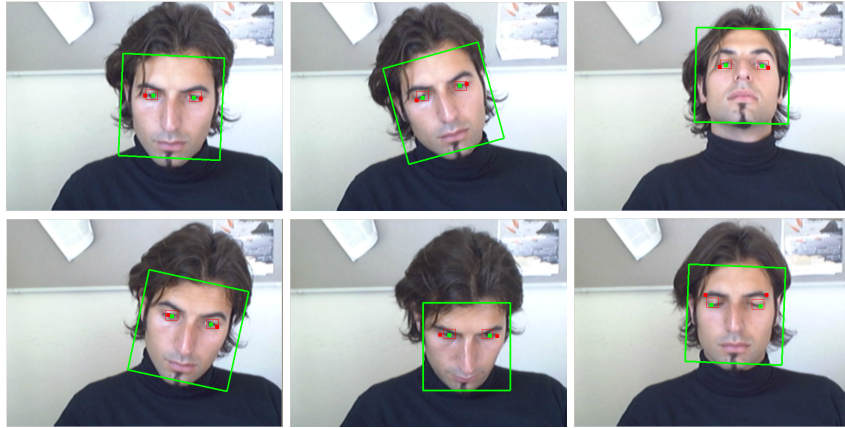
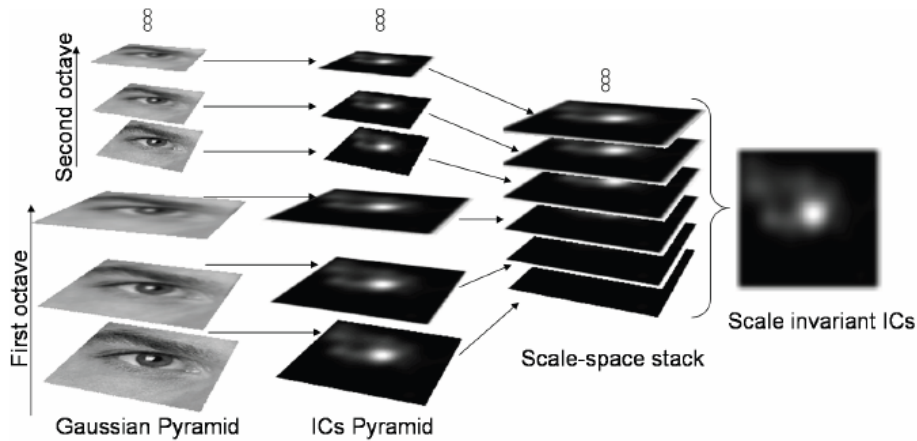


Fig. 4. Examples of combined eye center (green) and eye corner (red) detection

## 5 Scale Space Framework

Although the proposed approach is invariant to rotation and linear illumination changes, it still suffers from changes in scale. While in the previous work [15] the scale problem was solved by exhaustively searching for the scale value that obtained the best overall results, here we want to gain scale independence in order to avoid adjustments to the parameters for different situations. Firstly, since the sampled eye region depends on the scale of the detected face and on the camera resolution, to improve scale independency each eye region is scaled to a reference window. While this technique is expected to slightly decrease the accuracy with respect to the standard approach (due to interpolation artifacts), once the correct scale values are found for the chosen reference window, the algorithm can be applied at different scales without requiring an exhaustive parameter search. Furthermore, to increase robustness and accuracy, a scale space framework is used to select the isocenters that are stable across multiple scales.

The algorithm is applied to an input image at different scales and the outcome is analyzed for stable results. To this end, a Gaussian pyramid is constructed from the original grayscale image. The image is convolved with different Gaussians so that they are separated by a constant factor in scale space. In order to save computation, the image is downsampled into octaves. In each octave the isocenters are calculated at different intervals: for each of the image in the pyramid, the proposed method is applied by using the appropriate  $\sigma$  as a parameter for image derivatives. This procedure results in a isocenters pyramid (Figure 5). The responses in each octave are combined linearly, then scaled to the original reference size to obtain a scalespace stack. Every element of the scale space stack is considered equally important therefore they are simply summed into a single



**Fig. 5.** The scale space framework applied to eye location: the grayscale image is down-scaled to different octaves, each octave is divided into intervals. For each intervals, the centermap is computed and upscaled to a reference size to obtain a scale space stack. The combination of the obtained results gives the scale invariant isocenters.

centermap. The highest peaks in the resulting centermap will represent the most scale invariant isocenters.

## 6 Visual Gaze Estimation

Now that we have the eye center and corner location available, in order to correctly estimate visual gaze it would be reasonable to consider the head position and orientation to give a rough initialization of the visual gaze, and then use the information about the eye centers and corners to fine tune the information. Unfortunately, head pose estimators often involve many assumptions in order to achieve a realistic modeling (i.e. the shape and size of the head, the possible rotation angles of the eye, etc.). Furthermore, the high computational requirements of head pose estimators are not in line with the lightweight requirements of our system. Finally small mistakes in pose estimation might introduce additional errors in the final visual gaze estimation. Other methods tend to simplify the problem by assuming that the eye does not rotate but it just shifts. This assumption is reflected in commercial eye trackers, which deal with high resolution images of the eyes. This simplification comes from the assumption that the face is always frontal to the screen so the head pose information can be discarded. Therefore, we used the linear mapping method suggested by [19] and the user needs to perform a calibration procedure by looking at several known points on the screen. A 2D linear mapping is then constructed from the vector between the eye corner and the iris center and recorded at the known position on the screen. This vector is then used to interpolate between the known screen locations. For

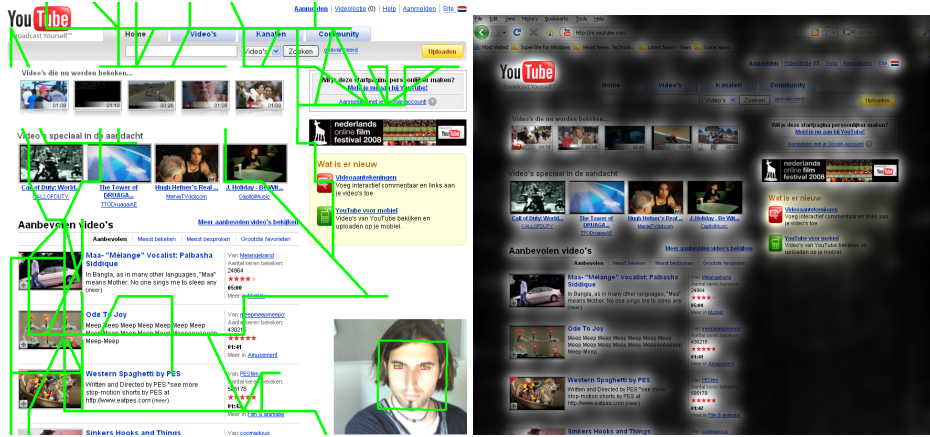


Fig. 6. Mapped visual gaze on an internet page and the associated heat map

example, if we have two calibration points  $P_1$  and  $P_2$  with screen coordinates  $\alpha$  and  $\beta$ , and eye-center vector (taken with origin from the anchor point)  $x$  and  $y$ , we can interpolate a new reading of the eye-center vector to obtain the screen coordinates by using the following interpolant:

$$\alpha = \alpha_1 + \frac{x - x_1}{x_2 - x_1}(\alpha_2 - \alpha_1) \quad (5)$$

$$\beta = \beta_1 + \frac{y - y_1}{y_2 - y_1}(\beta_2 - \beta_1) \quad (6)$$

The advantage of this approach is its low computational cost and a decent accuracy with respect to more complex systems. In fact the reported error introduced by this approximation is just  $1.2^\circ$ . Unfortunately, this method does not allow for large head movements, so the user will need to recalibrate in case of big horizontal or vertical shifts. However, in our case the distance from the screen and the camera parameters are known. So, we can compensate for this problem by remapping the calibration points accordingly with the registered displacement of the eyes. Therefore the final accuracy of the system is bounded just by the number of pixels that the eye is allowed to move. This generates some kind of *grid effect* on the recorded eye locations that can be seen in Figure 6.

While the final accuracy is bounded by the quality of the camera and the distance from it, we still believe that the system can be used for specific applications that do not require high level of accuracy (like changing the focused window or scrolling when looking outside the boundaries of the screen). The final outcome of the system can be visualized as a heat map (see Figure 6) which indicates the gaze patterns of the user. As can be seen from the figure our main goal is to use the system for qualitative investigation of the user interest while browsing a webpage and as such it is sufficient if we correctly identify the major sections of the webpage.



In order to evaluate the performance of our system, we asked 20 subjects to perform a simple task while looking at a webpage. The subjects were instructed to look and fixate at all the images displayed on a YouTube webpage (an example layout of such a page is displayed in Figure 6) starting from the higher left one and continuing to the right and below. We recorded the coordinates of their fixation and we checked if they fall within the corresponding image area. For such a simple task we obtained 95% accuracy.

In order to give the reader an idea of how our system is really working and its capabilities we have recorded two videos which can be accessed at:

<http://www.science.uva.nl/~rvalenti/downloads/tracker.wmv>

<http://www.science.uva.nl/~rvalenti/downloads/tracking.avi>

## 7 Conclusions

In this paper, we extended a method to infer eye center location to eye corner detection. Both eye center and eye corner can be detected at same time, do not require significant additional computation, and the detection can be scale invariant. We used the estimated locations to estimate the visual gaze of a user sitting in front of a screen. Although the accuracy of the system is bounded by the quality of the used webcam, we believe that the approximate gaze information can be useful for analyzing the gaze patterns of the subjects. The main advantage of our method is that it does not require any dedicated equipment, it does not use training which makes it very flexible, it is real-time, and it gives reasonable accuracy.

## References

1. COGAIN: Communication by gaze interaction, gazing into the future. <http://www.cogain.org> (2006)
2. Duchowski, A.T.: Eye Tracking Methodology: Theory and Practice. Springer (2007)
3. Bates, R., Istance, H., Oosthuizen, L., Majaranta, P.: Survey of de-facto standards in eye tracking. In: COGAIN Conf. on Comm. by Gaze Inter. (2005)
4. Asteriadis, S., Nikolaidis, N., Hajdu, A., Pitas, I.: An eye detection algorithm using pixel to edge information. In: Int. Symp. on Control, Commun. and Sign. Proc. (2006)
5. Bai, L., Shen, L., Wang, Y.: A novel eye location algorithm based on radial symmetry transform. In: ICPR. (2006) 511–514
6. Campadelli, P., Lanzarotti, R., Lipori, G.: Precise eye localization through a general-to-specific model definition. In: BMVC. (2006)
7. Cristinacce, D., Cootes, T.: Feature detection and tracking with constrained local models. In: BMVC. (2006)
8. Cristinacce, D., Cootes, T., Scott, I.: A multi-stage approach to facial feature detection. In: BMVC. (2004) 277–286
9. Hamouz, M., Kittlerand, J., Kamarainen, J.K., Paalanen, P., Kalviainen, H., Matas, J.: Feature-based affine-invariant localization of faces. PAMI **27**(9) (2005) 1490–1495

10. Türkan, M., Pardás, M., Çetin, E.: Human eye localization using edge projection. In: *Comp. Vis. Theory and App.* (2007)
11. Zhou, Z.H., Geng, X.: Projection functions for eye detection. In: *Pattern Recog.* (2004) 1049–1056
12. Lichtenauer, J., Hendriks, E., Reinders, M.: Isophote properties as features for object detection. In: *CVPR*. Volume 2. (2005) 649–654
13. Dam, E.B., ter Haar Romeny, B.: *Front End Vision and Multi-Scale Image Analysis*. Kluwer (2003)
14. van Ginkel, M., van de Weijer, J., van Vliet, L., Verbeek, P.: Curvature estimation from orientation fields. In: *SCIA*. (1999)
15. Valenti, R., Gevers, T.: Accurate eye center location and tracking using isophote curvature. In: *CVPR*. (June 2008)
16. Koenderink, J., van Doorn, A.J.: Surface shape and curvature scales. *Image and Vision Computing* (1992) 557–565
17. Comaniciu, D., Ramesh, V., Meer, P.: Kernel-based object tracking. *PAMI* **25**(5) (2003) 564–577
18. Zheng, Z., Yang, J., Yang, L.: A robust method for eye features extraction on color image. *Pattern Recognition Letters* **26** (2005) 2252–2261
19. Zhu, J., Yang, J.: Subpixel eye gaze tracking. In: *Face and Gesture Recogn. Conference*. (2002) 131