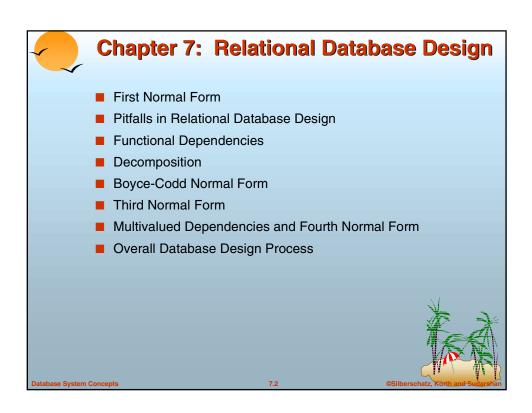
Chapter 7: Relational Database Design





First Normal Form

- Domain is atomic if its elements are considered to be indivisible units
 - ★ Examples of non-atomic domains:
 - ✓ Set of names, composite attributes
 - ✓ Identification numbers like CS101 that can be broken up into parts
- A relational schema R is in first normal form if the domains of all attributes of R are atomic
- Non-atomic values complicate storage and encourage redundant (repeated) storage of data
 - ★ E.g. Set of accounts stored with each customer, and set of owners stored with each account
 - ★ We assume all relations are in first normal form (revisit this in Chapter 9 on Object Relational Databases)

Database System Concepts

7.3





First Normal Form (Contd.)

- Atomicity is actually a property of how the elements of the domain are used.
 - ★ E.g. Strings would normally be considered indivisible
 - ★ Suppose that students are given roll numbers which are strings of the form CS0012 or EE1127
 - ★ If the first two characters are extracted to find the department, the domain of roll numbers is not atomic.
 - ★ Doing so is a bad idea: leads to encoding of information in application program rather than in the database.



Database System Concepts



Pitfalls in Relational Database Design

- Relational database design requires that we find a "good" collection of relation schemas. A bad design may lead to
 - * Repetition of Information.
 - ★ Inability to represent certain information.
- Design Goals:
 - * Avoid redundant data
 - ★ Ensure that relationships among attributes are represented
 - ★ Facilitate the checking of updates for violation of database integrity constraints.



Database System Concepts

7.5



Example

Consider the relation schema: Lending-schema = (branch-name, branch-city, assets, customer-name, loan-number, amount)

branch-name	branch-city	assets	customer- name	loan- number	amount
Downtown	Brooklyn	9000000	Jones	L-17	1000
Redwood	Palo Alto	2100000	Smith	L-23	2000
Perryridge	Horseneck	1700000	Hayes	L-15	1500
Downtown	Brooklyn	9000000	Jackson	L-14	1500

- Redundancy:
 - ★ Data for branch-name, branch-city, assets are repeated for each loan that a branch makes
 - ★ Wastes space
 - ★ Complicates updating, introducing possibility of inconsistency of assets value
- Null values
 - ★ Cannot store information about a branch if no loans exist
 - ★ Can use null values, but they are difficult to handle.

atabase System Concepts





Decomposition

- Decompose the relation schema *Lending-schema* into:

 Branch-schema = (branch-name, branch-city,assets)

 Loan-info-schema = (customer-name, loan-number, branch-name, amount)
- All attributes of an original schema (R) must appear in the decomposition (R_1 , R_2):

$$R = R_1 \cup R_2$$

Lossless-join decomposition.For all possible relations r on schema R

$$r = \prod_{\mathsf{R1}} (r) \bowtie \prod_{\mathsf{R2}} (r)$$



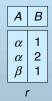
Database System Concepts

7.7



■ Decomposition of R = (A, B)

$$R_2 = (A) \qquad R_2 = (B)$$



$$\begin{bmatrix} \alpha \\ \beta \end{bmatrix}$$

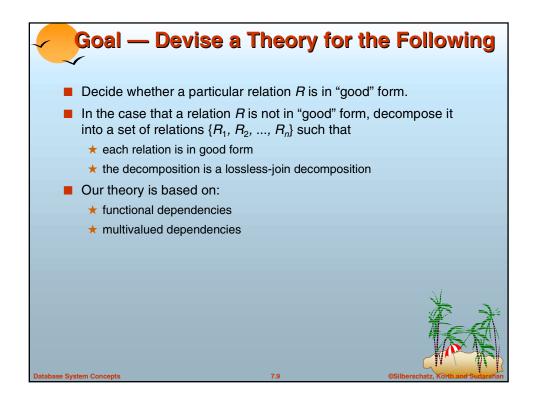
$$\Pi_{A}(r)$$

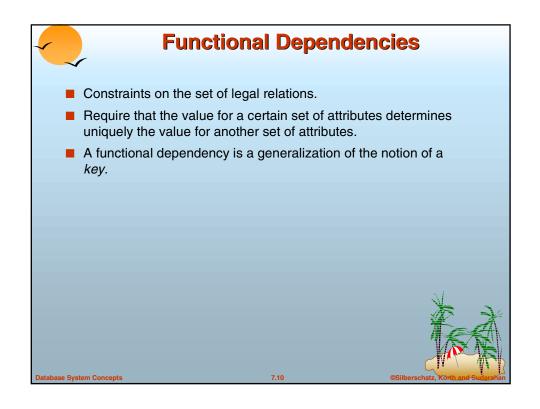
 $\prod_{A}\left(r\right) \bowtie\prod_{B}\left(r\right)$





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Functional Dependencies (Cont.)

■ Let R be a relation schema

$$\alpha \subseteq R$$
 and $\beta \subseteq R$

■ The functional dependency

$$\alpha \to \beta$$

holds on R if and only if for any legal relations r(R), whenever any two tuples t_1 and t_2 of r agree on the attributes α , they also agree on the attributes β . That is,

$$t_1[\alpha] = t_2[\alpha] \Rightarrow t_1[\beta] = t_2[\beta]$$

Example: Consider r(A,B) with the following instance of r.

■ On this instance, $A \rightarrow B$ does **NOT** hold, but $B \rightarrow A$ does hold



Database System Concepts

7.11



Functional Dependencies (Cont.)

- K is a superkey for relation schema R if and only if $K \rightarrow R$
- \blacksquare K is a candidate key for R if and only if

$$\star K \rightarrow R$$
, and

$$\star$$
 for no $\alpha \subset K$, $\alpha \to R$

■ Functional dependencies allow us to express constraints that cannot be expressed using superkeys. Consider the schema:

Loan-info-schema = (customer-name, loan-number, branch-name, amount).

We expect this set of functional dependencies to hold:

loan-number → amount loan-number → branch-name

but would not expect the following to hold:

loan-number → *customer-name*



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Use of Functional Dependencies

- We use functional dependencies to:
 - ★ test relations to see if they are legal under a given set of functional dependencies.
 - ✓ If a relation r is legal under a set F of functional dependencies, we say that r satisfies F.
 - ★ specify constraints on the set of legal relations
 - ✓ We say that F holds on R if all legal relations on R satisfy the set of functional dependencies F.
- Note: A specific instance of a relation schema may satisfy a functional dependency even if the functional dependency does not hold on all legal instances. For example, a specific instance of *Loan-schema* may, by chance, satisfy

loan-number \rightarrow customer-name.

Database System Concepts

7.13





Functional Dependencies (Cont.)

- A functional dependency is trivial if it is satisfied by all instances of a relation
 - ★ E.g.
 - ✓ customer-name, loan-number → customer-name
 - ✓ customer-name → customer-name
 - ★ In general, $\alpha \rightarrow \beta$ is trivial if $\beta \subseteq \alpha$



Database System Concepts



Closure of a Set of Functional Dependencies

- Given a set *F* set of functional dependencies, there are certain other functional dependencies that are logically implied by *F*.
 - \bigstar E.g. If A \to B and B \to C, then we can infer that A \to C
- The set of all functional dependencies logically implied by *F* is the *closure* of *F*.
- We denote the *closure* of *F* by F⁺.
- We can find all of F⁺ by applying Armstrong's Axioms:
 - \star if $\beta \subseteq \alpha$, then $\alpha \to \beta$

(reflexivity)

- \star if $\alpha \to \beta$, then $\gamma \alpha \to \gamma \beta$
- (augmentation)
- \star if $\alpha \to \beta$, and $\beta \to \gamma$, then $\alpha \to \gamma$ (transitivity)
- These rules are
 - ★ sound (generate only functional dependencies that actually hold) and
 - ★ complete (generate all functional dependencies that hold).



Database System Concepts

7.15

Silberschatz, Korth and Suda



Example

- R = (A, B, C, G, H, I)
 - $F = \{ A \rightarrow B \\ A \rightarrow C \}$
 - $CG \rightarrow H$
 - $CG \rightarrow I$
 - $B \rightarrow H$
- some members of F⁺
 - $\star A \rightarrow H$
 - \checkmark by transitivity from $A \rightarrow B$ and $B \rightarrow H$
 - $\bigstar AG \rightarrow I$
 - ✓ by augmenting $A \rightarrow C$ with G, to get $AG \rightarrow CG$ and then transitivity with $CG \rightarrow I$
 - ★ CG → HI
 - ✓ from $CG \rightarrow H$ and $CG \rightarrow I$: "union rule" can be inferred from
 - definition of functional dependencies, or
 - Augmentation of $CG \rightarrow I$ to infer $CG \rightarrow CGI$, augmentation of $CG \rightarrow H$ to infer $CGI \rightarrow HI$, and then transitivity

Database System Concepts

7.16

Silberschatz Korth



Procedure for Computing F⁺

■ To compute the closure of a set of functional dependencies F:

 $F^+ = F$ repeat

for each functional dependency f in F^+ apply reflexivity and augmentation rules on f add the resulting functional dependencies to F^+ for each pair of functional dependencies f_1 and f_2 in F^+ if f_1 and f_2 can be combined using transitivity then add the resulting functional dependency to F^+ until F^+ does not change any further

NOTE: We will see an alternative procedure for this task later



Database System Concepts

7.17



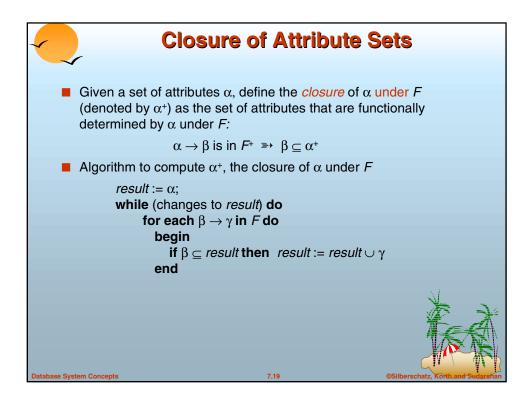
Closure of Functional Dependencies (Cont.)

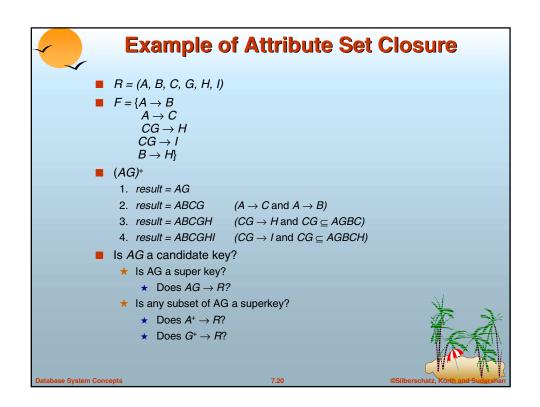
- We can further simplify manual computation of *F*⁺ by using the following additional rules.
 - \star If $\alpha \to \beta$ holds and $\alpha \to \gamma$ holds, then $\alpha \to \beta \gamma$ holds (union)
 - ★ If $\alpha \to \beta \gamma$ holds, then $\alpha \to \beta$ holds and $\alpha \to \gamma$ holds (decomposition)
 - ★ If $\alpha \to \beta$ holds and $\gamma \beta \to \delta$ holds, then $\alpha \gamma \to \delta$ holds (pseudotransitivity)

The above rules can be inferred from Armstrong's axioms.



atabase System Concepts







Uses of Attribute Closure

There are several uses of the attribute closure algorithm:

- Testing for superkey:
 - ★ To test if α is a superkey, we compute α^{+} and check if α^{+} contains all attributes of R.
- Testing functional dependencies
 - ★ To check if a functional dependency $\alpha \to \beta$ holds (or, in other words, is in F^+), just check if $\beta \subseteq \alpha^+$.
 - \star That is, we compute α ⁺ by using attribute closure, and then check if it contains β.
 - ★ Is a simple and cheap test, and very useful
- Computing closure of F
 - ★ For each $\gamma \subseteq R$, we find the closure γ^+ , and for each $S \subseteq \gamma^+$, we output a functional dependency $\gamma \to S$.

Database System Concept

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Canonical Cover

- Sets of functional dependencies may have redundant dependencies that can be inferred from the others
 - \star Eg: A \to C is redundant in: {A \to B, B \to C, A \to C}
 - ★ Parts of a functional dependency may be redundant

 ${\color{red} \nu}$ E.g. on RHS: $~\{A\rightarrow B,~B\rightarrow C,~A\rightarrow CD\}$ can be simplified to $~\{A\rightarrow B,~B\rightarrow C,~A\rightarrow D\}$

ightharpoonup E.g. on LHS: $\{A o B, \ B o C, \ AC o D\}$ can be simplified to

 $\{A \rightarrow B, B \rightarrow C, A \rightarrow D\}$

Intuitively, a canonical cover of F is a "minimal" set of functional dependencies equivalent to F, with no redundant dependencies or having redundant parts of dependencies



atabase System Concepts



Extraneous Attributes

- Consider a set F of functional dependencies and the functional dependency $\alpha \to \beta$ in F.
 - ★ Attribute A is extraneous in α if $A \in \alpha$ and F logically implies $(F \{\alpha \to \beta\}) \cup \{(\alpha A) \to \beta\}$.
 - ★ Attribute *A* is extraneous in β if $A \in \beta$ and the set of functional dependencies $(F \{\alpha \rightarrow \beta\}) \cup \{\alpha \rightarrow (\beta A)\}$ logically implies *F*.
- *Note:* implication in the opposite direction is trivial in each of the cases above, since a "stronger" functional dependency always implies a weaker one
- **Example:** Given $F = \{A \rightarrow C, AB \rightarrow C\}$
 - ★ B is extraneous in $AB \rightarrow C$ because $A \rightarrow C$ logically implies $AB \rightarrow C$.
- **Example:** Given $F = \{A \rightarrow C, AB \rightarrow CD\}$
 - ★ C is extraneous in AB → CD since A → C can be inferred everafter deleting C

Database System Concepts

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Testing if an Attribute is Extraneous

- Consider a set F of functional dependencies and the functional dependency $\alpha \to \beta$ in F.
 - ★ To test if attribute $A \in \alpha$ is extraneous in α
 - ✓ compute $(A \{\alpha\})^+$ using the dependencies in F
 - ✓ check that $(A \{\alpha\})^+$ contains α ; if it does, A is extraneous
 - ★ To test if attribute $A \in \beta$ is extraneous in β
 - \checkmark compute α^+ using only the dependencies in $F' = (F \{\alpha \to \beta\}) \cup \{\alpha \to (\beta A)\},$
 - \checkmark check that α^+ contains A; if it does, A is extraneous



Oatabase System Concepts



Canonical Cover

- \blacksquare A *canonical cover* for *F* is a set of dependencies F_c such that
 - \star F logically implies all dependencies in F_c and
 - \star F_c logically implies all dependencies in F, and
 - \star No functional dependency in F_c contains an extraneous attribute, and
 - \star Each left side of functional dependency in F_c is unique.
- To compute a canonical cover for *F*: repeat

Use the union rule to replace any dependencies in F $\alpha_1 \to \beta_1$ and $\alpha_1 \to \beta_1$ with $\alpha_1 \to \beta_1$ β_2 Find a functional dependency $\alpha \to \beta$ with an extraneous attribute either in α or in β If an extraneous attribute is found, delete it from $\alpha \to \beta$

until F does not change

■ Note: Union rule may become applicable after some extraneous attributes have been deleted, so it has to be re-applied

Database System Concepts

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Silberschatz, Korth and Sudars

Example of Computing a Canonical Cover

- R = (A, B, C) $F = \{A \rightarrow BC\}$
 - $B \rightarrow C$
 - $A \rightarrow B$ $AB \rightarrow C$
- Combine $A \rightarrow BC$ and $A \rightarrow B$ into $A \rightarrow BC$
 - ★ Set is now $\{A \rightarrow BC, B \rightarrow C, AB \rightarrow C\}$
- A is extraneous in $AB \rightarrow C$ because $B \rightarrow C$ logically implies $AB \rightarrow C$.
 - ★ Set is now $\{A \rightarrow BC, B \rightarrow C\}$
- C is extraneous in $A \to BC$ since $A \to BC$ is logically implied by $A \to B$ and $B \to C$.
- The canonical cover is:

$$A \rightarrow B$$

 $B \rightarrow C$



atabase System Concepts



Goals of Normalization

- Decide whether a particular relation *R* is in "good" form.
- In the case that a relation R is not in "good" form, decompose it into a set of relations $\{R_1, R_2, ..., R_n\}$ such that
 - ★ each relation is in good form
 - ★ the decomposition is a lossless-join decomposition
- Our theory is based on:
 - ★ functional dependencies
 - multivalued dependencies



Database System Concepts

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Decomposition

■ Decompose the relation schema *Lending-schema* into:

Branch-schema = (branch-name, branch-city, assets)

Loan-info-schema = (customer-name, loan-number,

branch-name, amount)

All attributes of an original schema (R) must appear in the decomposition (R₁, R₂):

$$R = R_1 \cup R_2$$

Lossless-join decomposition.

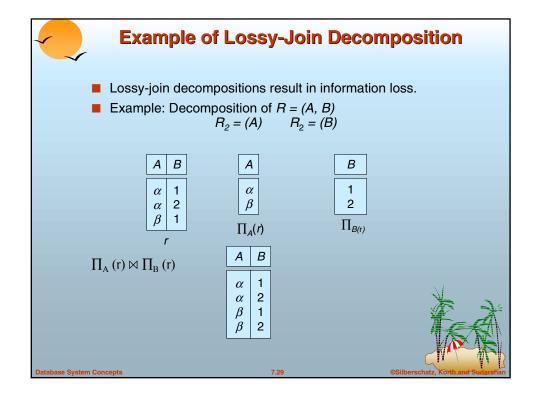
For all possible relations r on schema R

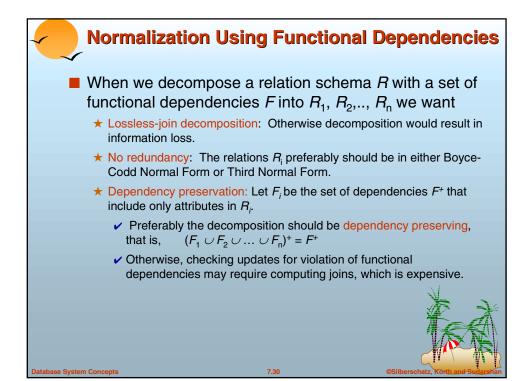
$$r = \prod_{\mathsf{R1}} (r) \bowtie \prod_{\mathsf{R2}} (r)$$

- A decomposition of R into R₁ and R₂ is lossless join if and only if at least one of the following dependencies is in F⁺:
 - $\star R_1 \cap R_2 \rightarrow R_1$
 - $\star R_1 \cap R_2 \rightarrow R_2$



atabase System Concepts







Example

- R = (A, B, C) $F = \{A \rightarrow B, B \rightarrow C\}$
- \blacksquare $R_1 = (A, B), R_2 = (B, C)$
 - ★ Lossless-join decomposition:

$$R_1 \cap R_2 = \{B\} \text{ and } B \rightarrow BC$$

- ★ Dependency preserving
- \blacksquare $R_1 = (A, B), R_2 = (A, C)$
 - ★ Lossless-join decomposition:

$$R_1 \cap R_2 = \{A\} \text{ and } A \to AB$$

★ Not dependency preserving (cannot check $B \rightarrow C$ without computing $R_1 \bowtie R_2$)



Database System Concepts

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Testing for Dependency Preservation

- To check if a dependency $\alpha \rightarrow \beta$ is preserved in a decomposition of R into R₁, R₂, ..., R_n we apply the following simplified test (with attribute closure done w.r.t. F)
 - \star result = α

while (changes to result) do

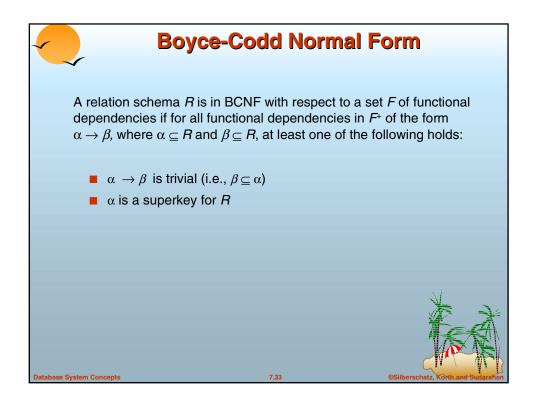
for each R_i in the decomposition

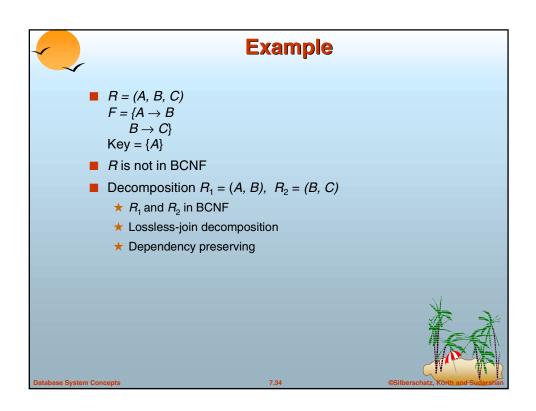
$$t = (result \cap R_i)^+ \cap R_i$$

- $result = result \cup t$
- \bigstar If *result* contains all attributes in $\beta,$ then the functional dependency $\alpha\to\beta$ is preserved.
- We apply the test on all dependencies in F to check if a decomposition is dependency preserving
- This procedure takes polynomial time, instead of the exponential time required to compute F^+ and $(F_1 \cup F_2 \cup ... \cup F_n)^+$

Database System Concepts









Testing for BCNF

- To check if a non-trivial dependency $\alpha \rightarrow \beta$ causes a violation of BCNF
 - 1. compute α^+ (the attribute closure of α), and
 - 2. verify that it includes all attributes of *R*, that is, it is a superkey of *R*.
- Simplified test: To check if a relation schema *R* with a given set of functional dependencies *F* is in BCNF, it suffices to check only the dependencies in the given set *F* for violation of BCNF, rather than checking all dependencies in *F*⁺.
 - ★ We can show that if none of the dependencies in F causes a violation of BCNF, then none of the dependencies in F⁺ will cause a violation of BCNF either
- However, using only F is incorrect when testing a relation in a decomposition of R
 - ★ E.g. Consider R (A, B, C, D), with $F = \{A \rightarrow B, B \rightarrow C\}$
 - ✓ Decompose R into $R_1(A,B)$ and $R_2(A,C,D)$
 - ✓ Neither of the dependencies in F contain only attributes from (A,C□) so we might be mislead into thinking R₂ satisfies BCNF.
 - ✓ In fact, dependency $A \rightarrow C$ in F⁺ shows R₂ is not in BCNF.

Database System Concepts

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BCNF Decomposition Algorithm

Note: each R_i is in BCNF, and decomposition is lossless-join.



Oatabase System Concepts



Example of BCNF Decomposition

- R = (branch-name, branch-city, assets, customer-name, loan-number, amount)
 F = {branch-name → assets branch-city loan-number → amount branch-name}
 Key = {loan-number, customer-name}
- Decomposition
 - $\star R_1$ = (branch-name, branch-city, assets)
 - \star R_2 = (branch-name, customer-name, loan-number, amount)
 - $\star R_3 = (branch-name, loan-number, amount)$
 - \star R_4 = (customer-name, loan-number)
- Final decomposition

 R_1, R_3, R_4



Database System Concepts

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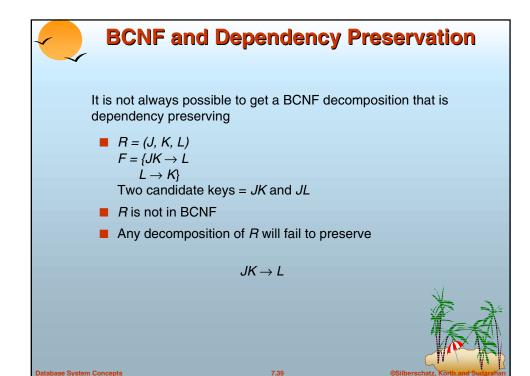


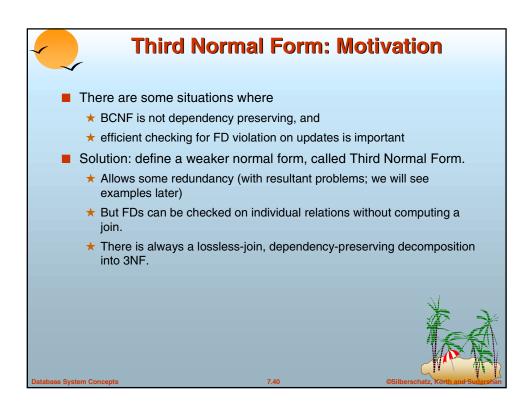
Testing Decomposition for BCNF

- \blacksquare To check if a relation R_i in a decomposition of R is in BCNF,
 - ★ Either test R_i for BCNF with respect to the restriction of F to R_i (that is, all FDs in F+ that contain only attributes from R_i)
 - ★ or use the original set of dependencies F that hold on R, but with the following test:
 - for every set of attributes $\alpha \subseteq R_i$, check that α ⁺ (the attribute closure of α) either includes no attribute of R_i , α , or includes all attributes of R_i .
 - ho If the condition is violated by some $\alpha \to \beta$ in F, the dependency $\alpha \to (\alpha^+ \alpha_-) \cap R_i$ can be shown to hold on R_i and R_i violates BCNF.
 - ✓ We use above dependency to decompose R_i



Database System Concepts







Third Normal Form

■ A relation schema *R* is in third normal form (3NF) if for all:

$$\alpha \rightarrow \beta$$
 in F^+

at least one of the following holds:

- $\star \alpha \rightarrow \beta$ is trivial (i.e., $\beta \in \alpha$)
- $\star \alpha$ is a superkey for R
- ★ Each attribute A in $\beta \alpha$ is contained in a candidate key for R. (NOTE: each attribute may be in a different candidate key)
- If a relation is in BCNF it is in 3NF (since in BCNF one of the first two conditions above must hold).
- Third condition is a minimal relaxation of BCNF to ensure dependency preservation (will see why later).



Database System Concepts

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3NF (Cont.)

- Example
 - \star R = (J, K, L) F = {JK \rightarrow L, L \rightarrow K}
 - ★ Two candidate keys: JK and JL
 - ★ R is in 3NF

 $JK \rightarrow L$ JK is a superkey

 $L \rightarrow K$ K is contained in a candidate key

- BCNF decomposition has (JL) and (LK)
 - Testing for $JK \rightarrow L$ requires a join
- There is some redundancy in this schema
- Equivalent to example in book:

Banker-schema = (branch-name, customer-name, banker-name)

 $banker\text{-}name \to branch \ name$

branch name customer-name \rightarrow banker-name



atabase System Concepts



Testing for 3NF

- Optimization: Need to check only FDs in F, need not check all FDs in F⁺.
- Use attribute closure to check, for each dependency $\alpha \to \beta$, if α is a superkey.
- If α is not a superkey, we have to verify if each attribute in β is contained in a candidate key of *R*
 - ★ this test is rather more expensive, since it involve finding candidate keys
 - ★ testing for 3NF has been shown to be NP-hard
 - ★ Interestingly, decomposition into third normal form (described shortly) can be done in polynomial time



Database System Concepts

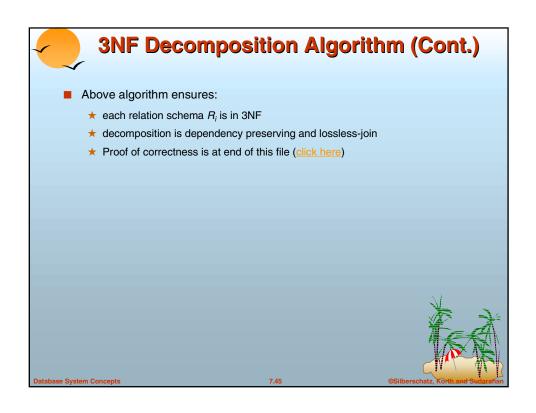
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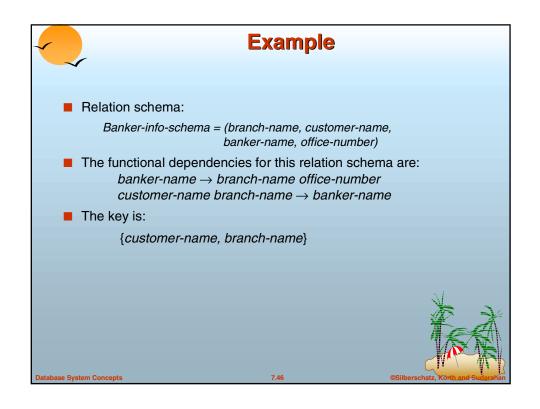


3NF Decomposition Algorithm

```
Let F_c be a canonical cover for F; i:=0; for each functional dependency \alpha \to \beta in F_c do if none of the schemas R_j, 1 \le j \le i contains \alpha \beta then begin i:=i+1; R_i:=\alpha \beta end if none of the schemas R_j, 1 \le j \le i contains a candidate key for R then begin i:=i+1; R_j:= any candidate key for R; end return (R_1, R_2, ..., R_j)
```

atabase System Concepts







Applying 3NF to Banker-info-schema

■ The **for** loop in the algorithm causes us to include the following schemas in our decomposition:

Banker-office-schema = (banker-name, branch-name, office-number)
Banker-schema = (customer-name, branch-name, banker-name)

Since Banker-schema contains a candidate key for Banker-info-schema, we are done with the decomposition process.



Database System Concepts

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Comparison of BCNF and 3NF

- It is always possible to decompose a relation into relations in 3NF and
 - ★ the decomposition is lossless
 - ★ the dependencies are preserved
- It is always possible to decompose a relation into relations in BCNF and
 - ★ the decomposition is lossless
 - ★ it may not be possible to preserve dependencies.



Database System Concepts



Comparison of BCNF and 3NF (Cont.)

- Example of problems due to redundancy in 3NF
 - \star R = (J, K, L) $F = \{JK \rightarrow L, L \rightarrow K\}$

J	L	K
j ₁	1,	<i>k</i> ₁
j_2	<i>I</i> ₁	<i>k</i> ₁
j_3	<i>I</i> ₁	<i>k</i> ₁
null	<i>l</i> ₂	<i>k</i> ₂

A schema that is in 3NF but not in BCNF has the problems of

- repetition of information (e.g., the relationship l_1 , k_1)
- need to use null values (e.g., to represent the relationship l_2 , k_2 where there is no corresponding value for J).

Database System Concepts

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Silberschatz Korth



Design Goals

- Goal for a relational database design is:
 - ★ BCNF.
 - ★ Lossless join.
 - ★ Dependency preservation.
- If we cannot achieve this, we accept one of
 - ★ Lack of dependency preservation
 - ★ Redundancy due to use of 3NF
- Interestingly, SQL does not provide a direct way of specifying functional dependencies other than superkeys.

Can specify FDs using assertions, but they are expensive to test

Even if we had a dependency preserving decomposition, using SQL we would not be able to efficiently test a functional dependency whose left hand side is not a key.

Database System Concepts

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Silberschatz Korth and Sudars



Testing for FDs Across Relations

- If decomposition is not dependency preserving, we can have an extra **materialized view** for each dependency $\alpha \rightarrow \beta$ in F_c that is not preserved in the decomposition
- The materialized view is defined as a projection on α β of the join of the relations in the decomposition
- Many newer database systems support materialized views and database system maintains the view when the relations are updated.
 - ★ No extra coding effort for programmer.
- The FD becomes a candidate key on the materialized view.
- Space overhead: for storing the materialized view
- Time overhead: Need to keep materialized view up to date when relations are updated

Database System Concepts

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Multivalued Dependencies

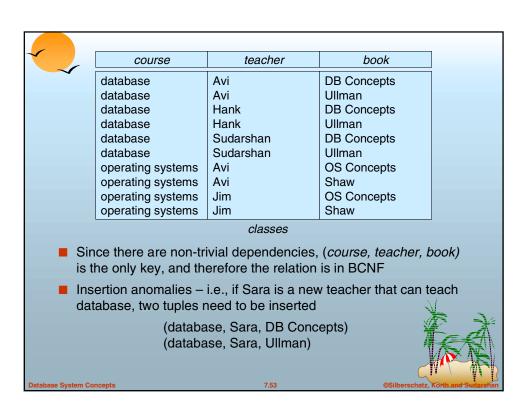
- There are database schemas in BCNF that do not seem to be sufficiently normalized
- Consider a database

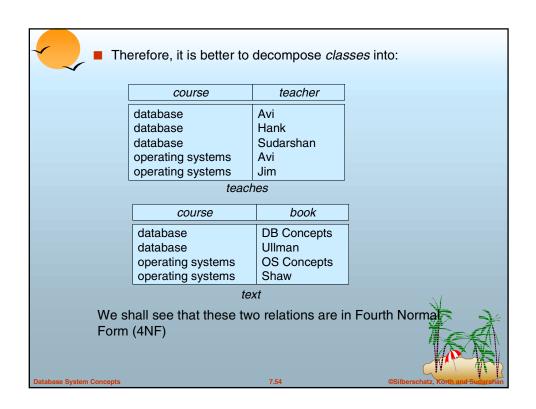
classes(course, teacher, book) such that $(c,t,b) \in classes$ means that t is qualified to teach c, and b is a required textbook for c

■ The database is supposed to list for each course the set of teachers any one of which can be the course's instructor, and the set of books, all of which are required for the course (no matter who teaches it).



Database System Concepts







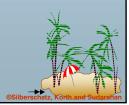
Multivalued Dependencies (MVDs)

Let R be a relation schema and let $\alpha \subseteq R$ and $\beta \subseteq R$. The *multivalued dependency*

$$\alpha \rightarrow \beta$$

holds on R if in any legal relation r(R), for all pairs for tuples t_1 and t_2 in r such that $t_1[\alpha] = t_2[\alpha]$, there exist tuples t_3 and t_4 in r such that:

$$\begin{array}{ll} t_1[\alpha] = t_2[\alpha] = t_3 \, [\alpha] \, t_4 \, [\alpha] \\ t_3[\beta] &= t_1 \, [\beta] \\ t_3[R \, -\beta] = \, t_2[R \, -\beta] \\ t_4 \, \beta] &= t_2[\beta] \\ t_4[R \, -\beta] = \, t_1[R \, -\beta] \end{array}$$



Database System Concepts

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MVD (Cont.)

■ Tabular representation of $\alpha \rightarrow \beta$

	α	β	$R-\alpha-\beta$
t_1	$a_1 \dots a_i$	$a_{i+1} \dots a_j$	$a_{j+1} \dots a_n$
t_2	$a_1 \dots a_i$	$b_{i+1} \dots b_j$	$b_{j+1} \dots b_n$
t_3	$a_1 \dots a_i$	$a_{i+1} \dots a_j$	$b_{j+1} \dots b_n$
t_4	$a_1 \dots a_i$	$b_{i+1} \dots b_j$	$a_{j+1} \dots a_n$



Database System Concepts



Example

■ Let *R* be a relation schema with a set of attributes that are partitioned into 3 nonempty subsets.

■ We say that $Y \rightarrow Z$ (Y multidetermines Z) if and only if for all possible relations r(R)

$$< y_1, z_1, w_1 > \in r \text{ and } < y_2, z_2, w_2 > \in r$$

then

$$< y_1, z_1, w_2 > \in r$$
 and $< y_1, z_2, w_1 > \in r$

Note that since the behavior of Z and W are identical it follows that $Y \rightarrow Z$ if $Y \rightarrow W$



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Example (Cont.)

In our example:

$$course \rightarrow \rightarrow teacher$$
 $course \rightarrow \rightarrow book$

- The above formal definition is supposed to formalize the notion that given a particular value of *Y* (*course*) it has associated with it a set of values of *Z* (*teacher*) and a set of values of *W* (*book*), and these two sets are in some sense independent of each other.
- Note:
 - \star If $Y \rightarrow Z$ then $Y \rightarrow Z$
 - ★ Indeed we have (in above notation) $Z_1 = Z_2$ The claim follows.



Database System Concepts



Use of Multivalued Dependencies

- We use multivalued dependencies in two ways:
 - To test relations to determine whether they are legal under a given set of functional and multivalued dependencies
 - 2. To specify constraints on the set of legal relations. We shall thus concern ourselves *only* with relations that satisfy a given set of functional and multivalued dependencies.
- If a relation r fails to satisfy a given multivalued dependency, we can construct a relations r' that does satisfy the multivalued dependency by adding tuples to r.



Database System Concepts

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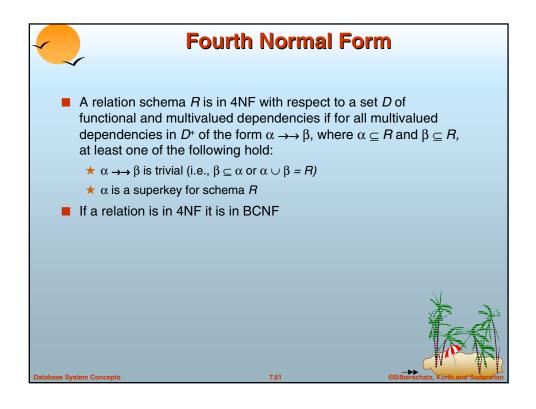
Theory of MVDs

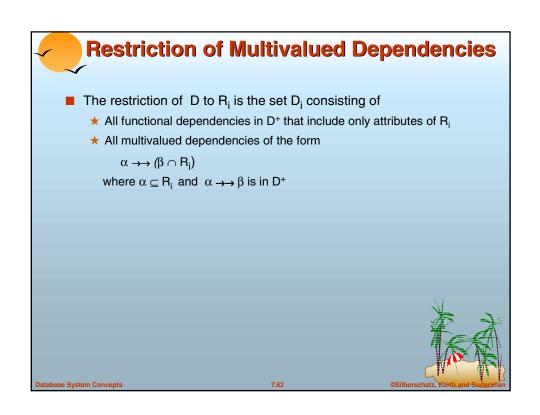
- From the definition of multivalued dependency, we can derive the following rule:
 - \star If $\alpha \rightarrow \beta$, then $\alpha \rightarrow \rightarrow \beta$

That is, every functional dependency is also a multivalued dependency

- The **closure** D⁺ of *D* is the set of all functional and multivalued dependencies logically implied by *D*.
 - ★ We can compute D+ from *D*, using the formal definitions of functional dependencies and multivalued dependencies.
 - ★ We can manage with such reasoning for very simple multivalued dependencies, which seem to be most common in practice
 - ★ For complex dependencies, it is better to reason about sets of dependencies using a system of inference rules (see Appendix)

Database System Concepts





```
Tesult: = {R}; done := false; compute D^+; Let D_i denote the restriction of D^+ to R_i while (not done)

If (there is a schema R_i in result that is not in 4NF) then begin

Let \alpha \rightarrow \beta be a nontrivial multivalued dependency that holds on R_i such that \alpha \rightarrow R_i is not in D_i, and \alpha \cap \beta = \phi; result := (result - R_i) \cup (R_i-\beta) \cup (\alpha, \beta); end

else done:= true;

Note: each R_i is in 4NF, and decomposition is lossless-join
```

```
Example
\blacksquare R = (A, B, C, G, H, I)
     F = \{ A \rightarrow \rightarrow B \}
              B \rightarrow \rightarrow HI
              CG \rightarrow \rightarrow H
\blacksquare R is not in 4NF since A \rightarrow B and A is not a superkey for R
Decomposition
    a) R_1 = (A, B)
                                                        (R_1 \text{ is in 4NF})
     b) R_2 = (A, C, G, H, I)
                                                       (R_2 \text{ is not in 4NF})
    c) R_3 = (C, G, H)
                                                       (R_3 \text{ is in 4NF})
    d) R_4 = (A, C, G, I)
                                                        (R_4 \text{ is not in 4NF})
■ Since A \rightarrow \rightarrow B and B \rightarrow \rightarrow HI, A \rightarrow \rightarrow HI, A \rightarrow \rightarrow I
    e) R_5 = (A, I)
                                                        (R_5 \text{ is in 4NF})
     f)R_6 = (A, C, G)
                                                        (R<sub>6</sub> is in 4NF)
```



Further Normal Forms

- **join dependencies** generalize multivalued dependencies
 - ★ lead to project-join normal form (PJNF) (also called fifth normal form)
- A class of even more general constraints, leads to a normal form called **domain-key normal form**.
- Problem with these generalized constraints: i hard to reason with, and no set of sound and complete set of inference rules.
- Hence rarely used



Database System Concepts

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Overall Database Design Process

- We have assumed schema R is given
 - ★ R could have been generated when converting E-R diagram to a set of tables.
 - ★ R could have been a single relation containing *all* attributes that are of interest (called **universal relation**).
 - ★ Normalization breaks *R* into smaller relations.
 - ★ R could have been the result of some ad hoc design of relations, which we then test/convert to normal form.



Database System Concepts



ER Model and Normalization

- When an E-R diagram is carefully designed, identifying all entities correctly, the tables generated from the E-R diagram should not need further normalization.
- However, in a real (imperfect) design there can be FDs from non-key attributes of an entity to other attributes of the entity
- E.g. *employee* entity with attributes *department-number* and *department-address*, and an FD *department-number* → *department-address*
 - ★ Good design would have made department an entity
- FDs from non-key attributes of a relationship set possible, but rare --- most relationships are binary



Database System Concepts

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Universal Relation Approach

- Dangling tuples Tuples that "disappear" in computing a join.
 - \star Let r_1 (R_1), r_2 (R_2),, r_n (R_n) be a set of relations
 - ★ A tuple r of the relation r_i is a dangling tuple if r is not in the relation:

$$\prod_{Ri} (r_1 \bowtie r_2 \bowtie ... \bowtie r_n)$$

■ The relation $r_1 \bowtie r_2 \bowtie ... \bowtie r_n$ is called a *universal relation* since it involves all the attributes in the "universe" defined by

$$R_1 \cup R_2 \cup ... \cup R_n$$

If dangling tuples are allowed in the database, instead of decomposing a universal relation, we may prefer to synthesize a collection of normal form schemas from a given set of attributes.



Database System Concepts



Universal Relation Approach

- Dangling tuples may occur in practical database applications.
- They represent incomplete information
- E.g. may want to break up information about loans into: (branch-name, loan-number)
 (loan-number, amount)
 (loan-number, customer-name)
- Universal relation would require null values, and have dangling tuples



Database System Concepts

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Universal Relation Approach (Contd.)

- A particular decomposition defines a restricted form of incomplete information that is acceptable in our database.
 - ★ Above decomposition requires at least one of customer-name, branch-name or amount in order to enter a loan number without using null values
 - ★ Rules out storing of customer-name, amount without an appropriate loan-number (since it is a key, it can't be null either!)
- Universal relation requires unique attribute names unique role assumption
 - ★ e.g. customer-name, branch-name
- Reuse of attribute names is natural in SQL since relation names can be prefixed to disambiguate names



atabase System Concepts



Denormalization for Performance

- May want to use non-normalized schema for performance
- E.g. displaying *customer-name* along with *account-number* and *balance* requires join of *account* with *depositor*
- Alternative 1: Use denormalized relation containing attributes of account as well as depositor with all above attributes
 - ★ faster lookup
 - ★ Extra space and extra execution time for updates
 - ★ extra coding work for programmer and possibility of error in extra code
- Alternative 2: use a materialized view defined as account ⋈ depositor
 - ★ Benefits and drawbacks same as above, except no extra coding work for programmer and avoids possible errors

Database System Concepts

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Other Design Issues

- Some aspects of database design are not caught by normalization
- Examples of bad database design, to be avoided:

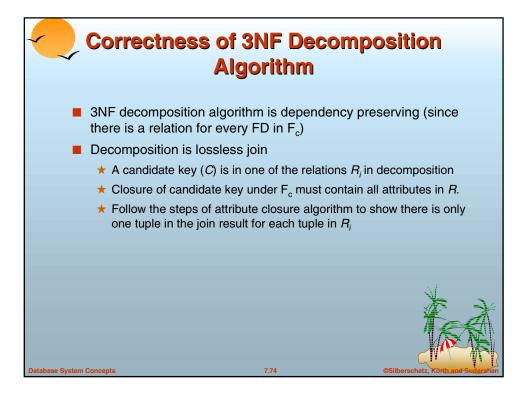
Instead of earnings(company-id, year, amount), use

- ★ earnings-2000, earnings-2001, earnings-2002, etc., all on the schema (company-id, earnings).
 - Above are in BCNF, but make querying across years difficult and needs new table each year
- company-year(company-id, earnings-2000, earnings-2001, earnings-2002)
 - Also in BCNF, but also makes querying across years difficult and requires new attribute each year.
 - Is an example of a crosstab, where values for one attribute become column names
 - ✓ Used in spreadsheets, and in data analysis tools

Database System Concepts



Proof of Correctness of 3NF Decomposition Algorithm





Correctness of 3NF Decomposition Algorithm (Contd.)

Claim: if a relation R_i is in the decomposition generated by the above algorithm, then R_i satisfies 3NF.

- Let R_i be generated from the dependency $\alpha \rightarrow \beta$
- Let $\gamma \rightarrow \beta$ be any non-trivial functional dependency on R_i . (We need only consider FDs whose right-hand side is a single attribute.)
- Now, *B* can be in either β or α but not in both. Consider each case separately.



Database System Concepts

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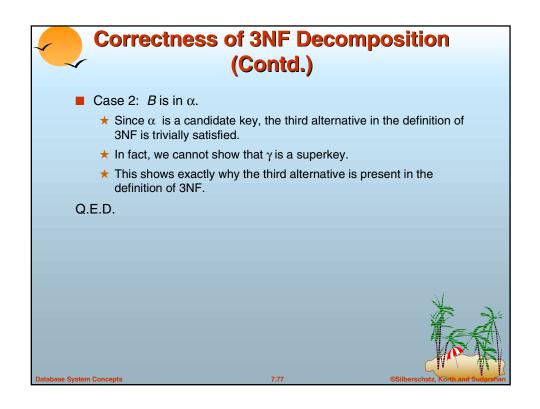


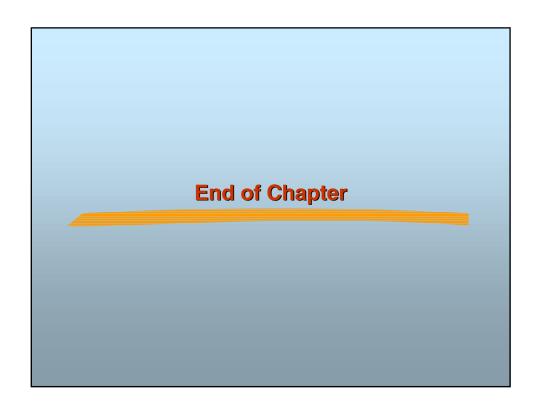
Correctness of 3NF Decomposition (Contd.)

- Case 1: If B in β:
 - \star If γ is a superkey, the 2nd condition of 3NF is satisfied
 - ★ Otherwise α must contain some attribute not in γ
 - ★ Since $\gamma \rightarrow$ B is in F⁺ it must be derivable from F_c, by using attribute closure on γ .
 - \star Attribute closure not have used $\alpha \to \beta$ if it had been used, α must be contained in the attribute closure of γ , which is not possible, since we assumed γ is not a superkey.
 - ★ Now, using $\alpha \rightarrow (\beta \{B\})$ and $\gamma \rightarrow B$, we can derive $\alpha \rightarrow B$ (since $\gamma \subseteq \alpha$ β , and $\beta \notin \gamma$ since $\gamma \rightarrow B$ is non-trivial)
 - ★ Then, *B* is extraneous in the right-hand side of $\alpha \rightarrow \beta$; which is not possible since $\alpha \rightarrow \beta$ is in F_c .
 - Thus, if B is in β then γ must be a superkey, and the second condition of 3NF must be satisfied.

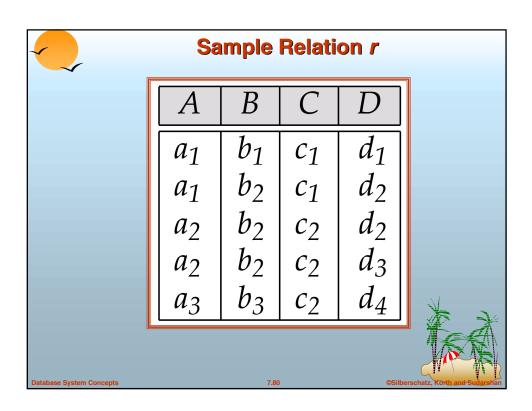
Database System Concepts







branch-name	branch-city	assets	customer- name	loan- number	атоип
		,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,	-		
Downtown	Brooklyn Palo Alto	9000000	Jones Smith	L-17 L-23	1000 2000
Redwood			01111111		
Perryridge Downtown	Horseneck	1700000	Hayes	L-15 L-14	1500 1500
	Brooklyn	9000000	Jackson		
Mianus	Horseneck	400000	Jones	L-93	500
Round Hill	Horseneck	8000000	Turner	L-11	900
Pownal	Bennington	300000	Williams	L-29	1200
North Town	Rye	3700000	Hayes	L-16	1300
Downtown	Brooklyn	9000000	Johnson	L-18	2000
Perryridge	Horseneck	1700000	Glenn	L-25	2500
Brighton	Brooklyn	7100000	Brooks	L-10	2200



The customer Relation					
	customer-name	customer-street	customer-city		
	Jones	Main	Harrison		
	Smith	North	Rye		
	Hayes	Main	Harrison		
	Curry	North	Rye		
	Lindsay	Park	Pittsfield		
	Turner	Putnam	Stamford		
	Williams	Nassau	Princeton		
	Adams	Spring	Pittsfield		
	Johnson	Alma	Palo Alto		
	Glenn	Sand Hill	Woodside		
	Brooks	Senator	Brooklyn		
	Green	Walnut	Stamford	x I	
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